

CBCS Scheme

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15MAT21

Second Semester B.E. Degree Examination, Dec.2016/Jan.2017 Engineering Mathematics - II

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing one full question from each module.

Module-1

- 1 a. Solve $(D-2)^2 y = 8(e^{2x} + x + x^2)$ by inverse differential operator method. (06 Marks)
b. Solve $(D^2 - 4D + 3)y = e^x \cos 2x$, by inverse differential operator method. (05 Marks)
c. Solve by the method of variation of parameters $y'' - 6y' + 9y = \frac{e^{3x}}{x^2}$. (05 Marks)

OR

- 2 a. Solve $(D^2 - 1)y = x \sin 3x$ by inverse differential operator method. (06 Marks)
b. Solve $(D^3 - 6D^2 + 11D - 6)y = e^{2x}$ by inverse differential operator method. (05 Marks)
c. Solve $(D^2 + 2D + 4)y = 2x^2 + 3e^{-x}$ by the method of undetermined coefficient. (05 Marks)

Module-2

- 3 a. Solve $x^3 y''' + 3x^2 y'' + xy' + 8y = 65 \cos(\log x)$. (06 Marks)
b. Solve $xy p^2 + p(3x^2 - 2y^2) - 6xy = 0$. (05 Marks)
c. Solve the equation $y^2(y - xp) = x^4 p^2$ by reducing into Clairaut's form, taking the substitution $x = \frac{1}{x}$ and $y = \frac{1}{y}$. (05 Marks)

OR

- 4 a. Solve $(2x + 3)^2 y'' - (2x + 3)y' - 12y = 6x$. (06 Marks)
b. Solve $p^2 + 4x^5 p - 12x^4 y = 0$. (05 Marks)
c. Solve $p^3 - 4xy p + 8y^2 = 0$. (05 Marks)

Module-3

- 5 a. Obtain the partial differential equation by eliminating the arbitrary function. $Z = f(x + at) + g(x - at)$. (06 Marks)
b. Solve $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$, for which $\frac{\partial z}{\partial y} = -2 \sin y$, when $x = 0$ and $z = 0$, when y is an odd multiple of $\frac{\pi}{2}$. (05 Marks)
c. Find the solution of the wave equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$ by the method of separation of variables. (05 Marks)

OR

- 6 a. Obtain the partial differential equation by eliminating the arbitrary function $\ell x + my + nz = \phi(x^2 + y^2 + z^2)$. (06 Marks)
b. Solve $\frac{\partial^2 z}{\partial y^2} = z$, given that, when $y = 0$, $z = e^x$ and $\frac{\partial z}{\partial y} = e^{-x}$. (05 Marks)

- c. Derive one dimensional heat equation $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$. (05 Marks)

Module-4

- 7 a. Evaluate $\int_{-1}^1 \int_0^z \int_{x-z}^{x+z} (x+y+z) dy dx dz$. (06 Marks)
- b. Evaluate $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} xy dy dx$ by changing the order of integration. (05 Marks)
- c. Evaluate $\int_0^4 x^{3/2} (4-x)^{5/2} dx$ by using Beta and Gamma function. (05 Marks)

OR

- 8 a. Evaluate $\int_0^\infty \int_0^\infty e^{-(x^2+y^2)} dx dy$ by changing to polar co-ordinates. Hence show that $\int_0^\infty e^{-x^2} dx = \sqrt{\frac{\pi}{2}}$. (06 Marks)
- b. Find by double integration, the area lying inside the circle $r = a \sin \theta$ and outside the cardioid $r = a(1 - \cos \theta)$. (05 Marks)
- c. Obtain the relation between beta and gamma function in the form $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$. (05 Marks)

Module-5

- 9 a. Find i) $L\{e^{-3t}(2 \cos 5t - 3 \sin 5t)\}$ ii) $L\left\{\frac{\cos at - \cos bt}{t}\right\}$. (06 Marks)
- b. If a periodic function of period $2a$ is defined by $f(t) = \begin{cases} t & \text{if } 0 \leq t \leq a \\ 2a - t & \text{if } a \leq t \leq 2a \end{cases}$ then show that $L\{f(t)\} = \frac{1}{s^2} \tan h\left(\frac{as}{2}\right)$. (05 Marks)
- c. Solve the equation by Laplace transform method. $y''' + 2y'' - y' - 2y = 0$. Given $y(0) = y'(0) = 0, y''(0) = 6$. (05 Marks)

OR

- 10 a. Find $L^{-1}\left\{\frac{s+3}{s^2-4s+13}\right\}$. (06 Marks)
- b. Find $L^{-1}\left\{\frac{s}{(s^2+a^2)^2}\right\}$ by using Convolution theorem. (05 Marks)
- c. Express $f(t) = \begin{cases} \sin t, & 0 \leq t < \pi \\ \sin 2t, & \pi \leq t < 2\pi \\ \sin 3t, & t \geq 2\pi \end{cases}$ in terms of unit step function and hence find its Laplace transforms. (05 Marks)

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